

# *Al - Muhandis*

*Journal of The Iraqi Society of Engineers - Serial -145 - 2001*

*No. 1 / March - 2001*



# Al-Muhandis

Volume 145 No.1 March 2001

Iraqi Society of Engineers

BAGHDAD

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## Solar Thermal Modeling Of A Non -Air Conditioned Room With A Southern Thermal Storage Walls

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## التمثيل الحراري لبناية غير مكيفة ذات جدران جنوبية خازنة للحرارة

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### Abstract

In this paper a drum water wall consists of metallic containers filled with water. Outer surface of this wall is blackened and glazed, while the inner surface is directly contact with a massive wall. With the help of appropriate energy balance conditions, the Fourier equation of heat conduction has been solved to drive the explicit expression for the indoor temperature and heat-flux entering the living space as a function of time. Since the ambient temperature and solar radiation vary periodically, the periodic solution for equation of heat conduction has been considered in the analysis. This lead to closed form solutions.

The effect of drum water depth, massive wall and thickness are studied in this paper. Numerical calculations have been carried out for a typical cold day in Baghdad on 21- January-2000.

It is found that the average indoor temperature and heat flux into the living space is maximum for water-concrete configuration.

### الخلاصة

في هذه الدراسة تم استحداث جدار خازن للحرارة يتكون من جدار مائي مبني من حاويات معدنية صغيرة مملوءة بالماء. السطح الخارجي لهذا الجدار ذو لون اسود و مغطى بطبقة من الزجاج، في حين أن السطح الداخلي في حالة تماس مباشر مع جدار الغرفة الجنوبي.

تم حل معادلة فورير لانتقال الحرارة باتجاه واحد خلال جدار مستوي باستخدام ظروف موازنة حرارية مناسبة. و من خلال الحل تم الحصول على صيغة حل رياضي محدد لتغير الحرارة الداخلية والحرارة المنتقلة إلى الغرفة. وبما إن درجة الحرارة الخارجية والإشعاع الشمسي يتغيران زمنيا. لذلك تم اعتبار إن الحرارة المنتقلة إلى البناية خلال تركيبها تتغير زمنيا أيضا.

تم دراسة تأثير سمك الجدار المائي و مواد بناء الجدار الجنوبي و سمكه على الأداء الحراري للغرفة، كذلك تم إجراء حسابات رقمية ليوم ٢١ من شهر كانون الثاني لعام ٢٠٠٠. ومن خلال الحسابات تم التوصل إلى إن معدل درجة الحرارة الداخلية و معدل الحرارة المنتقلة إلى الغرفة خلال الجدار الجنوبي في حدهما الأعلى لجدار على هيئة ماء + كونكريت.



## 1. Introduction

Energy conservation in buildings is usually perceived as reducing energy consumption, whether the conserved energy is renewable or nonrenewable. A Trombe wall represents a simple way of collecting solar energy and stored it release the energy to the living space at later time. Then simply Trombe wall can be regarded as conservation system.

A Trombe wall is a thick wall built up either by concrete or stone. The outer surface of the wall is painted dark to absorbed solar energy and stored as a sensible heat within the wall and transferred it by conduction through the wall and by convection and radiation to the living space.

A water wall is considered as a liquid thermal storage medium, which is based on the same considerations as massive Trombe wall. In water wall, drums of water are arranged up one above the other behind the collector glazing. The solar energy is absorbed by water drums and converted into heat, stored heat in the water and transferred by convective and radiation to the living space.

In this communication a drum water wall consist of metallic containers with water. One surface of the wall is blackened and glazed, while the another surface is directly contact with a massive wall.

The water concrete configuration is assumed as a southern wall of a room, and the effect of water depth, massive wall materials and the thickness on the room thermal performance are studied.

## 2. Analysis

A building room of rectangular shape, with dimensions of 6m long, 5m wide and 4m height, based on the ground is considered. The following reasonable a assumptions are made.

- i. All walls except southern walls are of identical materials and the same thickness as in reference (1).
- ii. The southern wall is consist of outer glass sheet of 6mm thickness, cavity, water column and massive wall.
- iii. The roof of identical materials as in reference (2).
- iv. Heat flow in the walls and roof is always transverse to their surface area.
- v. The inside air temperature is uniform in space through the room.
- vi. Steady state heat transfer through the window.
- vii. The outer surfacer of walls and roof are exposed to solar radiation and ambient air which are assumed as a periodic function of time.
- viii. The outside are temperature for all walls/roof is assumed in fairly true for a building of moderate height.

### 2.1 Periodic Heat Flux Through Walls and Roof

The temperature distribution in the walls and roof is characterized by one-dimensional heat conduction equation.

$$\frac{\partial^2 T_{j,t,x}}{\partial X^2} = \frac{1}{\alpha_j} \cdot \frac{\partial T_{j,t,x}}{\partial t} \quad (1)$$



Where  $\alpha_j$  is the thermal diffusivity of the  $j$ th wall/roof material and can be expressed as :

$$\alpha_j = \frac{K_j}{\rho_j \cdot C_j}$$

Equation (1) can be solved by separation of variables techniques as<sup>[3]</sup> :

$$T_{j,t,x} = A_{0j} \cdot x_j + B_{0j} +$$

$$\sum_{m=1}^6 \left( A_{j,m} \cdot e^{\gamma_{j,m} \cdot X_j} + B_{j,m} \cdot e^{-\gamma_{j,m} \cdot X_j} \right) e^{imw} \quad (2)$$

Where:

$$\gamma_{j,m} = \sqrt{\frac{i \cdot m \cdot w}{\alpha_j}}$$

Where:

$$w = \frac{2\pi}{24} (h^{-1})$$

### 2.1.1 Periodic Heat Flux Through Southern Wall

A schematic sketch for the southern wall is shown figure (1). The heat conduction equation (1) is supplemented with following boundary conditions:

at  $X = 0$

$$-K_3 \cdot \frac{dT_{3,t,x}}{dx} = hw(TW_t - T_{3,t,x}) \quad (3)$$

Where  $TW_t$  is the water column temperature and can be expressed by fourier series as<sup>[7]</sup>:

$$TW_t = T_{wo} + \sum_{m=1}^6 TWM_m \cdot e^{imwt} \quad (4)$$

at  $X=X_3$

$$-K_3 \frac{dT_{3,t,x}}{dx} = h_2 [T_{3,t,x} - T_{Room,t}] \quad (5)$$

Where  $T_{Room,t}$  is the indoor temperature and can be expressed by Fourier series as<sup>[7]</sup>:

$$T_{Room,t} = T_{O1} + \sum_{m=1}^6 T_{O2,m} \cdot e^{imwt} \quad (6)$$

The heat balance of water column is:

$$M_w C_w \frac{dT_{W,t}}{dt} = h_1 (SOAT_{j,t} - T_{W,t}) - hw(T_{W,t} - T_{3,t,x}) \quad (7)$$

Where  $SOAT_{j,t}$  is solar temperature of  $j$ th wall/roof and can be calculated by equation [4]:

$$SOAT_{j,t} = TAM_t + \frac{\alpha_j \cdot SRA_{j,t}}{h_1} - \frac{\epsilon_j \cdot \Delta R_j}{h_1} \quad (8)$$

Where  $TAM_t$  and  $SRA_{j,t}$  are the ambient air temperature and solar radiation incident on  $j$ th wall and roof. They can be expressed by Fourier series as:

$$TAM_t = T_{Ao} + \sum_{m=1}^6 TT_m \cdot e^{imwt} \quad (9)$$

$$SRA_{j,t} = S_{o_j} + \sum_{m=1}^6 S_{j,m} \cdot e^{imwt} \quad (10)$$



equation (8) can be expressed by Fourier series as:

$$SOAT_{j,T} = TSO_j + \sum_{m=1}^6 TSM_{j,m} \cdot e^{-im\omega t} \quad (11)$$

Substituting equation 2, 4, 6, 9, 10, and 11 in equation 3, 5 and 7 the constants TWo and TWm can be found as:

$$TWO = UT_3 \left[ \left[ \frac{1}{h_1} + \frac{X_3}{K_3} + \frac{1}{h_w} \right] TSO_3 + \left[ \frac{1}{h_w} - \frac{1}{h_2} \right] TO_1 \right] \quad (12)$$

$$TWM_m = \frac{h_1 \cdot TSM_{3,m} + HC5_m TO2_m}{HC4_m} \quad (13)$$

Where:

$$\frac{1}{UT_3} = \frac{1}{h_1} + \frac{1}{h_w} + \frac{X_3}{K_3} + \frac{1}{h_2} \quad (14)$$

The heat flux through the southern wall to the living space is given by the equation:

$$Q_{3,t} = h_2 (T_{j,t,x} - T_{Room,t}) \quad (15)$$

Equation (15) can be written as:

$$Q_{3,t} = UT_3 (TSO_3 - TO_1) + \sum_{m=1}^6 (HC8_m TO2_m + HC9_m TSM_{3,m}) e^{-im\omega t} \quad (16)$$

The constants HCO<sub>m</sub> to HC9<sub>m</sub> are listed in the appendix (1).

### 2.1.2 Heat Flux Thoug Another Walls And Roof

$$Q_{3,j} = h_2 (T_{j,t,x} - T_{Room,t}) \quad (17)$$

### 2.2 Heat Conduction into the Ground [4]

$$Q_{g,t} = K_g \cdot A_g \left. \frac{\partial T(y,t)}{\partial y} \right|_{y=0} \quad (18)$$

where T<sub>(y,t)</sub> is the ground temperature distribution which can be obtained by solving equation (1) after replacing (y) instead of (x).

### 2.3 Heat Transfer through Window [4]

$$Q_{w,t} = \alpha_w \cdot \tau_w \cdot A_w \cdot SRA_{j,t} - h_3 [T_{Room,t} - TAM_t] A_w \quad (19)$$

Where the first term of equation 19 represent the direct absorption of solar radiation transmitted through the east-facing window and the second term is the net convection-radiation heat transfer loss through the window.

### 2.4 Total Heat Loss Due to Air Infiltration [5]

$$Q_{vt} = Ma \cdot Wo [T_{Room,t} - TAM_t] + Wo \cdot \Delta H \cdot M_a \quad (20)$$

Where the first term of equation (20) represent the sensible heat due to temperature difference between indoor and outdoor, while the second term is the latent



heat due the difference in enthalpy between indoor and outdoor air.

**2.5 Heat Balance for the Room Air**

The net heat balance for the internal air of the room is:

$$MaCa \frac{dT_{Room,t}}{dt} = \left[ \sum_{j=1}^4 Q_{j,t} \right] + Q_{3,t} + Q_{wt} - Q_{gt} - Q_{vt} \tag{21}$$

Substituting equation 16, 17, 18, 19, and 20 into equation 21, the constants TO<sub>1</sub> and TO<sub>2m</sub> can be found as:

$$TO_1 = \frac{\sum_{j=2}^5 (U_j \cdot TS_{O_j} \cdot A_j) + (UT_3 - U_3)TS_{O_3} \cdot A_3 + U_j \cdot TS_{O_j} \cdot A_j}{\left( \sum_{j=2}^5 U_j \cdot A_j \right) + (UT_3 - U_3)A_3 + U_j \cdot A_j}$$

$$TO_{2m} = \frac{\left( \sum_{j=2}^5 H_{12,j,m} \cdot TSM_{j,m} \cdot A_j \right) + (Hc_{9,m} - H_{12,j,m})TSM_{3,m} \cdot A_3 + BS_{18,j,m} \cdot A_j}{imwt \cdot MaCa - \sum_{j=2}^5 (H_{11,j,m} A_j) + (H_{11,j,m} - HC_{8,j,m})A_3 \cdot BS_{17,j,m} \cdot A_j}$$

The constant H<sub>11j,m</sub>, H<sub>12j,m</sub>, BS<sub>17j,m</sub>, BS<sub>18j,m</sub> are listed in appendix(2).

**3. Results and Discussion**

The hourly variation of solar intensity [6] on different walls, roof and ambient temperature have been shown in figure (2).

Figure (3) shows the effect of water column depth on the indoor temperature. It is seen from the figure that the water depth has a weak effect on the indoor temperature. Therefore a depth of 0.1m seemed to be suitable.

Figure (4) shows the effect of concrete thickness in water-concrete wall on the indoor temperature. It is seen from the

figure that as the concrete thickness decreases the maximum and mean daily indoor temperature increases, therefore, when the water column thickness is 0.1m and the concrete thickness is 0.1m also, the maximum indoor temperature is equal to 13.5 °C, while it is equal to 13.2 °C when the concrete thickness is equal to 0.15m.

Figure (5) shows the variation of heat flux to the room from the southern wall for different valued of concrete thickness. It is seen from the figure that the maximum heat flux to the room from southern wall is equal to 1880 KJ/hr, when the concrete thickness is equal to 0.1m, while it is equal to 1650 KJ/hr when the concrete thickness to 0.3m, therefore the heat flux to the room from southern wall can be increased by 2.5, 6, 9 and 15% as a result of reducing the concrete thickness from 0.3m to 0.25, 0.2, 0.15 and 0.1m respectively.

Figure (6) and (7) show the effect of constructional materials and thickness on the indoor temperature and inside surface temperature of southern wall respectively. It is seen from the figures that concrete gives always higher indoor temperature and higher inside surface temperature compared with that for brick and concrete. While light concrete gives lower indoor and inside surface temperature of southern wall. From these figure it is that then wall gives better thermal performance to the room.

Figure (8) shows the variation of heat flux to the room from southern wall to the living space for different constructional material of the wall. It is seen from the figure that concrete wall gives maximum heat flux of 1880 KJ/hr. while brick wall



gives 1650 KJ/hr and light concrete gives 1450 KJ/hr all of then 0.1m thickness for water depth.

#### 4. Conclusions

The calculations have been corresponding to a typical winter day at January 21 at Baghdad. Although to general conclusions for all ranges of meteorological parameters can be drawn the predictions for a single day, it is instructive to summarize to qualitative features of results as follows:

- 1- The average indoor temperature and heat flux into the living space is maximum for water wall of 0.1m water depth and 0.1m concrete thickness.
- 2- Water concrete configurations is most suited among other than constructional materials.
- 3- The fluctuation of indoor temperature of the sun is significantly reduced as compared to the observed by Khalifa et al [2].
- 4- It is obvious that the establishment of this technology will change the appearance of future buildings and is a real challenge for architects.

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## Nomenclature

$h_w$	Heat transfer coefficient between the plates and water KJ/hr. $m^2$ . $^{\circ}C$ .
$T_{w_t}$	Water temperature $^{\circ}C$ .
$h_2$	Heat transfer coefficient between mass wall and air of living space KJ/hr. $m^2$ . $^{\circ}C$ .
$T_{room_t}$	Room temperature $^{\circ}C$ .
$M_w$	Mass of water wall Kg.
$C_w$	Specific heat of water KJ/Kg. $^{\circ}C$ .
$h_1$	Heat transfer coefficient between absorbing and air in sun space of water wall KJ/hr. $m^2$ . $^{\circ}C$ .
$SOAT_{i,t}$	Solar temperature of the walls and roof $^{\circ}C$ .
$TAM_t$	Readable data of ambient air temperature $^{\circ}C$ .
$\alpha_j$	Absorptivity of the walls and roof
$SRA_{i,t}$	Solar intensity on walls and roof KJ/hr. $m^2$ .
$\epsilon_j$	Emissivity of the walls and roof.
$\Delta R_j$	Different between long wave radiation incident on surface from sky and the radiation KJ/hr. $m^2$ .
$TAO$	Average value of ambient air temperature $^{\circ}C$ .
$T_m$	Amplitude of mth harmonic of water temperature $^{\circ}C$ .
$So_j$	Average value of solar intensity KJ/hr. $m^2$ .
$S_{i,m}$	Amplitude of mth harmonic of $So_j$ KJ/hr. $m^2$ .
$T_{soj}$	Average value of solar temperature $^{\circ}C$ .
$TSM_{i,m}$	Amplitude of mth harmonic of $T_{soj}$ $^{\circ}C$ .
$TW_o$	Average value of water temperature $^{\circ}C$ .
$X_j$	Total thickness of walls and roof m
$K_j$	Thermal conductivity of walls and roof KJ/hr. m. $^{\circ}C$ .
$K_g$	Thermal conductivity of ground KJ/hr. m. $^{\circ}C$ .
$A_g$	Area of ground $m^2$ .
$Y$	Coordinate normal to the ground m.
$\alpha$	Absorptivity of the glass.
$\tau_w$	Transmittance of the glass.
$A_w$	Area of window $m^2$ .
$h_3$	Heat transfer coefficient between the inside air and ambient air through window glass KJ/hr. $m^2$ . $^{\circ}C$ .
$M_a$	Mass of inside air Kg.
$C_a$	Specific heat of air KJ/Kg. $^{\circ}C$ .
$W_o$	Hourly air change due to the door and window openings air change per hour.
$\Delta H$	Latent heat due to the different in humidity of the outdoor and indoor air KJ/ $m^3$
$t$	Time coordinate hr.
$j$	1, 2, 3, 4, 5, correspond to roof, east, south, west, north wall respectively.



Appendix (1)

$$HC0_m = \frac{1 - \frac{h_2}{K\gamma_{j,m}}}{1 + \frac{h_2}{K\gamma_{j,m}}} e^{-2\gamma_m \ell}$$

$$F0_m = \frac{1 - \frac{h_2}{K\gamma_{j,m}}}{1 + \frac{h_2}{K\gamma_{j,m}}} e^{-2\gamma_m \ell}$$

$$HC1_m = \frac{1 + \frac{hw_2}{K\gamma_m}}{1 - \frac{hw_2}{K\gamma_m}}$$

$$F1_m = \frac{\frac{hw_2}{K\gamma_{j,m}}}{1 - \frac{hw_2}{K\gamma_{j,m}}}$$

$$HC2_m = \frac{F0_m}{HC1_m - HC0_m}$$

$$F2_m = \frac{F1_m}{HC1_m - HC0_m}$$

$$HC3_m = HC1_m \cdot HC2_m$$

$$F3_m = hc0_m \cdot F2_m$$

$$HC4_m = Mw \cdot Cw \cdot i \cdot m \cdot \omega + h_{eff} + hw_2 - F3_m - F2_m$$

$$HC5_m = hw_2(HC3_m + HC2_m)$$

$$F4_m = \frac{h_{eff} \cdot F3_m}{HC4_m}$$

$$HC6_m = \frac{HC3_m \cdot HC4_m + F3_m \cdot HC5_m}{HC4_m}$$

$$F5_m = \frac{h_{eff} \cdot F2_m}{HC4_m}$$

$$HC7_m = \frac{HC2_m \cdot HC4_m + F2_m \cdot HC5_m}{HC4_m}$$

$$\frac{1}{h_{eff}} = \frac{1}{hw_1} + \frac{1}{h_1}$$

$$U_T = \frac{1}{\frac{1}{h_1} + \frac{1}{hw_1} + \frac{1}{hw_2} + \frac{\ell}{K} + \frac{1}{h_2}}$$

$$HC8_m = HC6_m e^{\gamma_m \cdot \ell} + HC7_m e^{-\gamma_m \cdot \ell} - 1$$

$$HC9_m = F4_m e^{\gamma_m \cdot \ell} + F5_m e^{-\gamma_m \cdot \ell}$$



## Appendix (2) CONSTANTS OF FOUR-LAYERED ROOF

The roof is consist from cement tile of 30mm thickness, dry sand 10cm thickness, concrete of 15cm thickness and gypsum 20mm thickness.

$$\beta_{j,m} = \sqrt{\frac{i.m.\omega.\rho1_j.C1_j}{K1_j}}$$

$$\alpha_{j,m} = \sqrt{\frac{i.m.\omega.\rho2_j.C2_j}{K2_j}}$$

$$\phi_{j,m} = \sqrt{\frac{i.m.\omega.\rho3_j.C3_j}{K3_j}}$$

$$\gamma_{j,m} = \sqrt{\frac{i.m.\omega.\rho3_j.C3_j}{K3_j}}$$

$$BS0_{j,m} = \frac{1 - \frac{h2}{K4_j \cdot \gamma_{j,m}}}{1 + \frac{h2}{K4_j \cdot \gamma_{j,m}}} \cdot e^{-2\gamma_{j,m} \cdot x4_j}$$

$$BS1_{j,m} = B0_{j,m} \cdot e^{\gamma_{j,m} \cdot x3_j} + e^{-\gamma_{j,m} \cdot x3_j}$$

$$BS2_{j,m} = \frac{K4_j \cdot \gamma_{j,m}}{K3_j \cdot \phi_{j,m}} \cdot [B0_{j,m} \cdot e^{\gamma_{j,m} \cdot x3_j} - e^{-\gamma_{j,m} \cdot x3_j}]$$

$$BS3_{j,m} = \frac{1}{2} \cdot (B1_{j,m} + B2_{j,m}) \cdot e^{-\phi_{j,m} \cdot x3_j}$$

$$BS4_{j,m} = \frac{1}{2} \cdot (B1_{j,m} - B2_{j,m}) \cdot e^{\phi_{j,m} \cdot x3_j}$$

$$BS5_{j,m} = (B3_{j,m} \cdot e^{\phi_{j,m} \cdot x2_j} - B4_{j,m} \cdot e^{-\phi_{j,m} \cdot x2_j})$$

$$BS6_{j,m} = \frac{K3_j \cdot \phi_{j,m}}{K2_j \cdot \alpha_{j,m}} \cdot [B3_{j,m} \cdot e^{\phi_{j,m} \cdot x2_j} - B4_{j,m} \cdot e^{-\phi_{j,m} \cdot x2_j}]$$

$$BS7_{j,m} = \frac{1}{2} \cdot (B5_{j,m} + B6_{j,m}) \cdot e^{-\alpha_{j,m} \cdot x2_j}$$



$$BS8_{j,m} = \frac{1}{2} \cdot (B5_{j,m} - B6_{j,m}) \cdot e^{\alpha_{j,m} \cdot x2_j}$$

$$BS9_{j,m} = (B7_{j,m} \cdot e^{\alpha_{j,m} \cdot x2_j} + B8_{j,m} \cdot e^{\alpha_{j,m} \cdot x2_j})$$

$$BS10_{j,m} = \frac{K2_j \cdot \alpha_{j,m}}{K1_j \cdot \beta_{j,m}} \cdot [B7_{j,m} \cdot e^{\alpha_{j,m} \cdot x1_j} - B8_{j,m} \cdot e^{-\alpha_{j,m} \cdot x1_j}]$$

$$BS11_{j,m} = \frac{1}{2} \cdot (B9_{j,m} + B10_{j,m}) \cdot e^{-\beta_{j,m} \cdot x1_j}$$

$$BS12_{j,m} = \frac{1}{2} \cdot (B9_{j,m} - B10_{j,m}) \cdot e^{\beta_{j,m} \cdot x_j}$$

$$BS13_{j,m} = \left(1 - \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot C11_{j,m} - \left(1 + \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot C12_{j,m}$$

$$BS14_{j,m} = \left(1 + \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot B12_{j,m} - \left(1 - \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot B11_{j,m}$$

$$BS15_{j,m} = \left[ \begin{array}{l} \left(1 - \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot (B0_{j,m} \cdot C11_{j,m} - B11_{j,m} \cdot C0_{j,m}) \\ - \left(1 + \frac{h1_j}{K1_j \cdot \beta_{j,m}}\right) \cdot (B0_{j,m} \cdot C12_{j,m} - B12_{j,m} \cdot C0_{j,m}) \end{array} \right]$$

$$BS16_{j,m} = \frac{B13_{j,m}}{B14_{j,m}}$$

$$BS17_{j,m} = h2 \cdot \left( \frac{B16_{j,m} \cdot e^{\gamma_{j,m} \cdot x4_j} + B13_{j,m} \cdot e^{-\gamma_{j,m} \cdot x4_j}}{B14_{j,m}} - 1 \right)$$

$$BS18_{j,m} = \frac{h1_j \cdot h2}{K1_j \cdot \beta_j} \cdot \left( \frac{B0_{j,m} \cdot e^{\gamma_{j,m} \cdot x4_j} + e^{-\gamma_{j,m} \cdot x4_j}}{B14_{j,m}} - 1 \right)$$



$$H0_{j,m} = \frac{\frac{h2}{K4_j \cdot \gamma_{j,m}^4} \cdot e^{-\gamma_{j,m} \cdot x_{4j}}}{1 + \frac{h2}{K4_j \cdot \gamma_{j,m}}}$$

$$H1_{j,m} = (C0_{j,m} \cdot e^{\gamma_{j,m} \cdot x_{3j}})$$

$$H2_{j,m} = \frac{K4_j \cdot \gamma_{j,m}}{K3_j \cdot \phi_{j,m}} \cdot [C0_{j,m} \cdot e^{\gamma_{j,m} \cdot x_j}]$$

$$H3_{j,m} = \frac{1}{2} \cdot (C1_{j,m} + C2_{j,m}) \cdot e^{-\phi_{j,m} \cdot x_{3j}}$$

$$H4_{j,m} = \frac{1}{2} \cdot (C1_{j,m} - C2_{j,m}) \cdot e^{\phi_{j,m} \cdot x_{3j}}$$

$$H5_{j,m} = (C3_{j,m} \cdot e^{\phi_{j,m} \cdot x_{2j}} - C4_{j,m} \cdot e^{-\phi_{j,m} \cdot x_{2j}})$$

$$H6_{j,m} = \frac{K3_j \cdot \phi_{j,m}}{K2_j \cdot \alpha_{j,m}} \cdot [C3_{j,m} \cdot e^{\phi_{j,m} \cdot x_{2j}} - C4_{j,m} \cdot e^{-\phi_{j,m} \cdot x_{2j}}]$$

$$H7_{j,m} = \frac{1}{2} \cdot (C5_{j,m} + C6_{j,m}) \cdot e^{-\alpha_{j,m} \cdot x_{2j}}$$

$$H8_{j,m} = \frac{1}{2} \cdot (C5_{j,m} - C6_{j,m}) \cdot e^{\alpha_{j,m} \cdot x_{2j}}$$

$$H9_{j,m} = (C7_{j,m} \cdot e^{\alpha_{j,m} \cdot x_{2j}} + C8_{j,m} \cdot e^{-\alpha_{j,m} \cdot x_{2j}})$$

$$H10_{j,m} = \frac{K2_j \cdot \alpha_{j,m}}{K1_j \cdot \beta_{j,m}} \cdot [C7_{j,m} \cdot e^{\alpha_{j,m} \cdot x_{1j}} - C8_{j,m} \cdot e^{-\alpha_{j,m} \cdot x_{1j}}]$$

$$H11_{j,m} = \frac{1}{2} \cdot (C9_{j,m} + C10_{j,m}) \cdot e^{-\beta_{j,m} \cdot x_{1j}}$$

$$H12_{j,m} = \frac{1}{2} \cdot (C9_{j,m} - C10_{j,m}) \cdot e^{\beta_{j,m} \cdot x_{1j}}$$



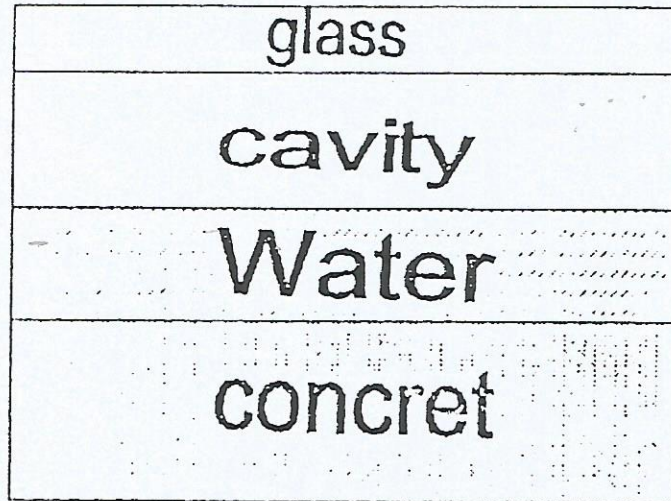


Figure (1): Water Wall

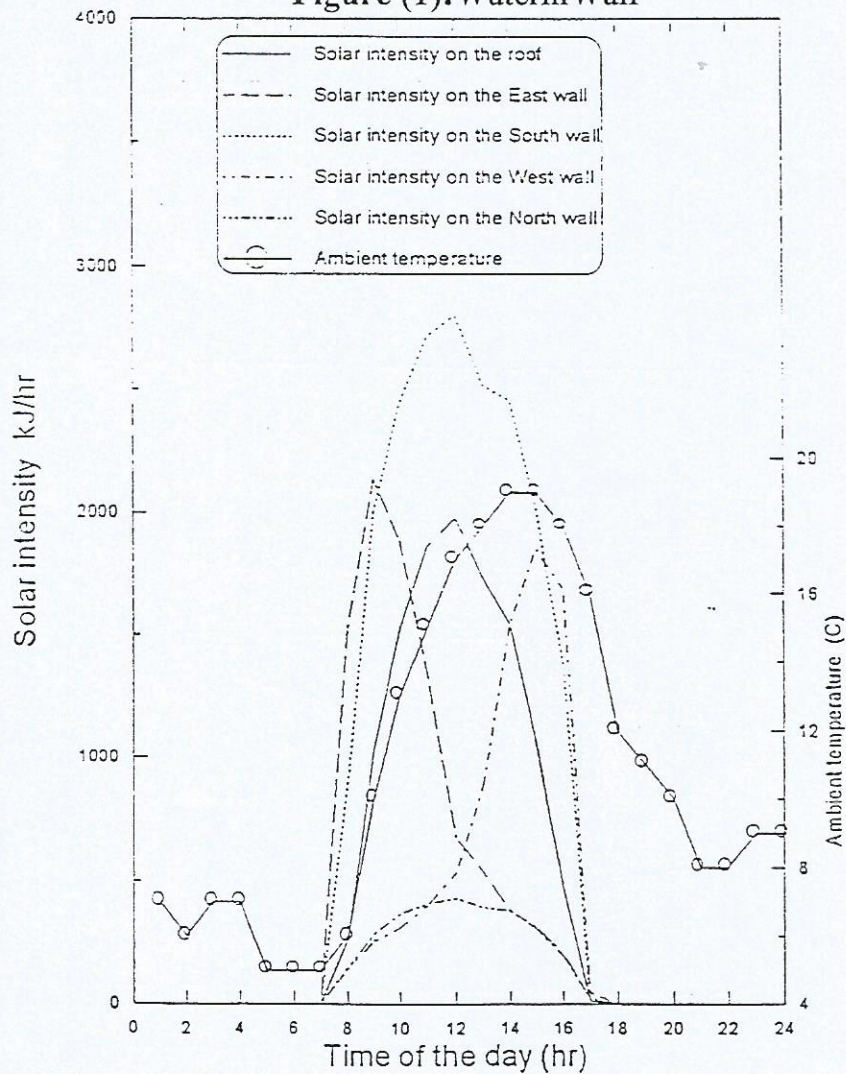


Figure (2): Ambient temperature and solar intensity on walls of various orientation for Baghdad on January.



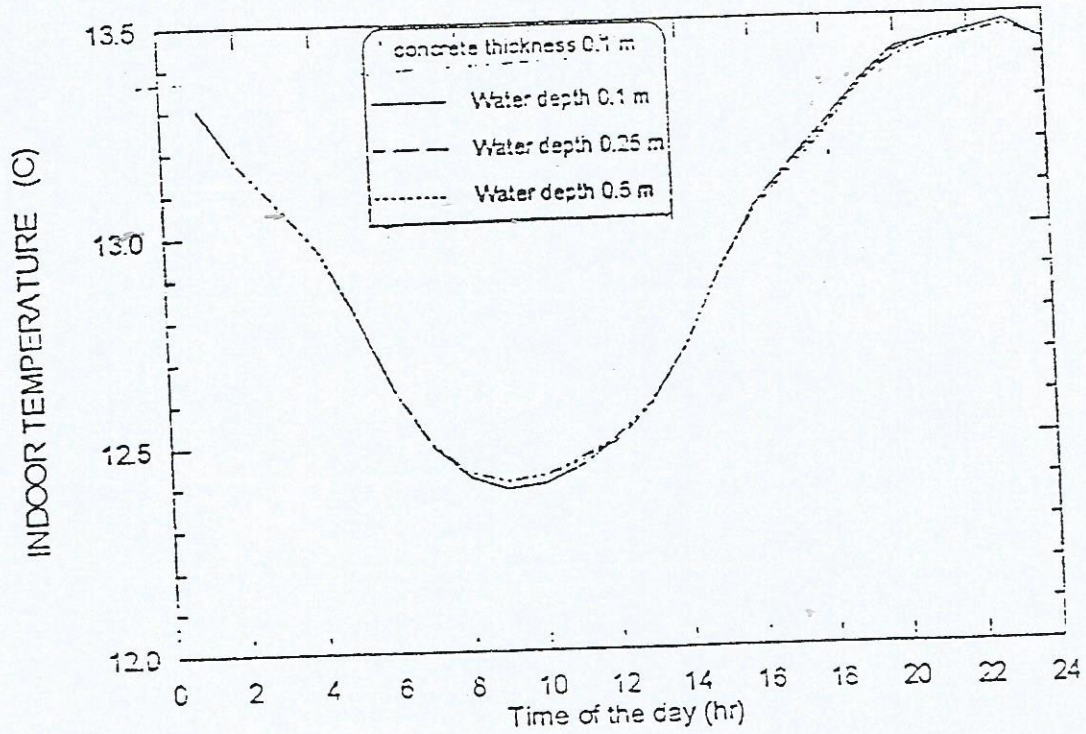


Figure (3): Effect of water depth of the water wall on the indoor temperature

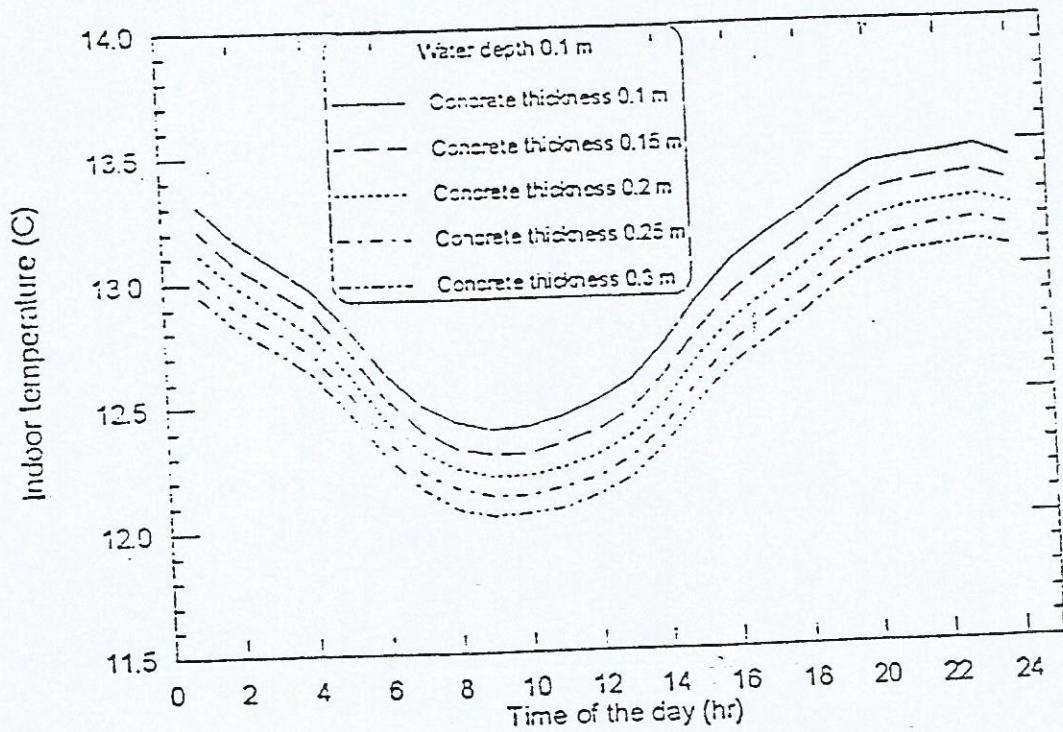


Figure (4): Effect of concrete thickness of the water wall on the indoor temperature



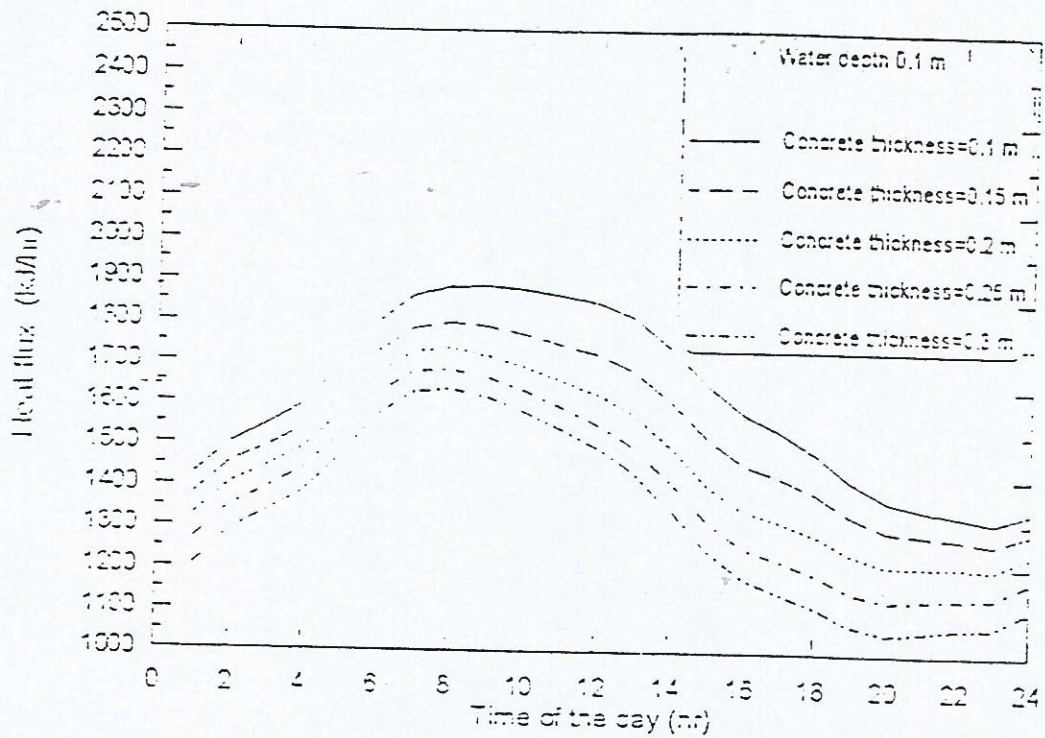


Figure (5): Heat flux to the room from the water wall for different concrete thickness

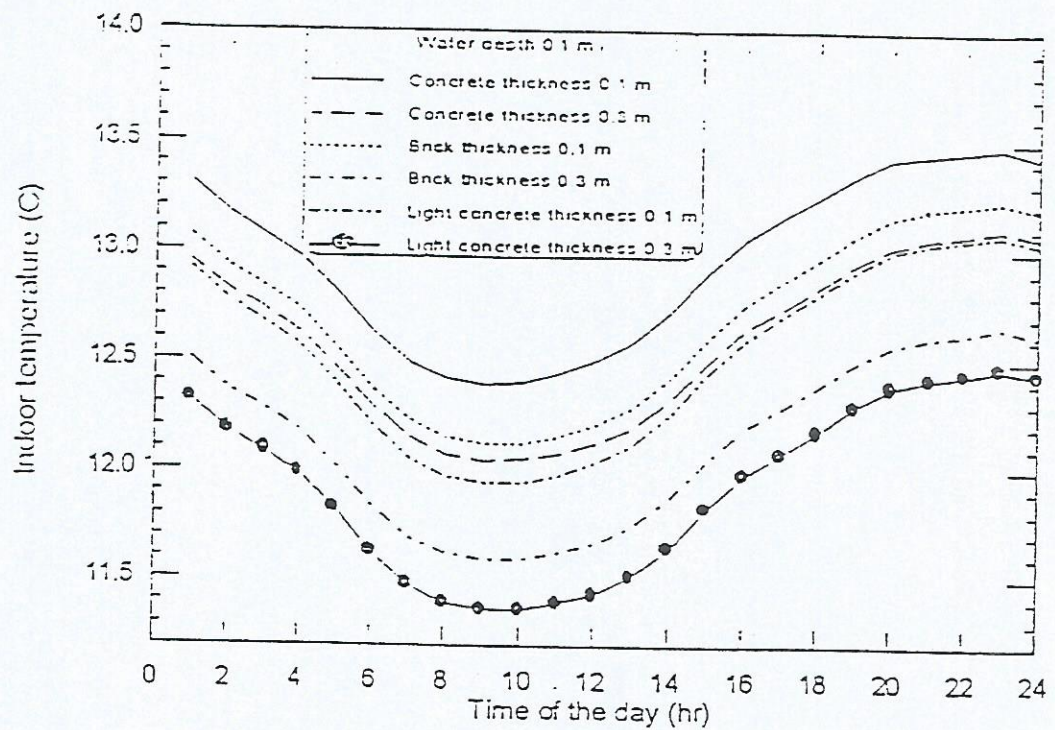


Figure (6): Effect of wall materials of the water wall on the indoor temperature



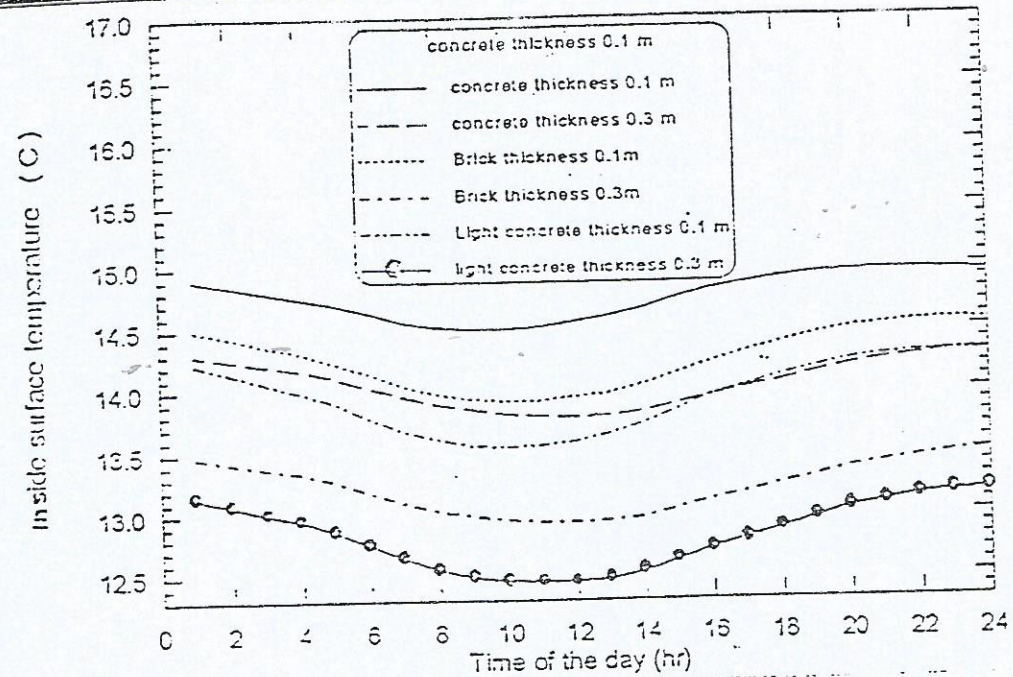


Figure (7): Effect of building materials on the inside surface temperature of the inside wall

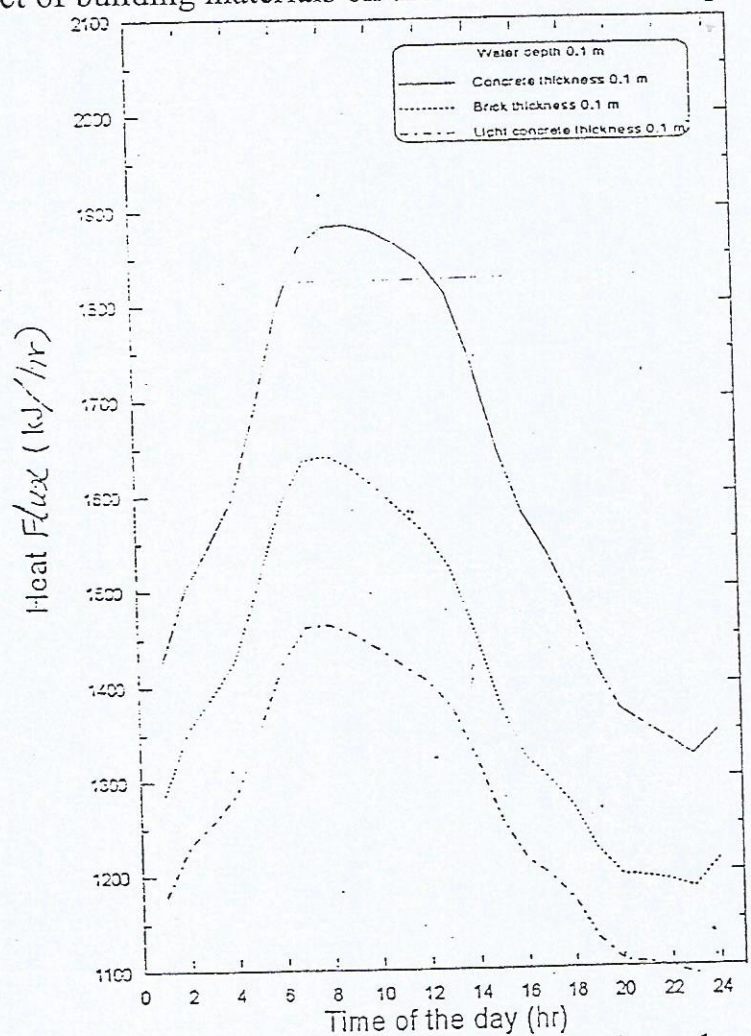


Figure (8): Hourly variation of heat flux to the room through water wall of different building materials