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MINISTRY OF HIGHER EDUCATION  
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AL-MUSTANSIRIAH UNIVERSITY  
COLLEGE OF SCIENCE  
DEPARTMENT OF MATHEMATICS*

*NECESSARY CONDITION  
FOR OPTIMAL CONTROL  
OF DYNAMICAL SYSTEMS*

*A THESIS*

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*Abstract:*

In this work, we have studied and analyzed the following non-linear dynamical systems:

$$\begin{cases} \dot{x}(t) = f(t, x(t), u(t)) \\ x(0) = x_0 \\ x(1) = x_1 \end{cases}$$

Augmented with the following cost functional

$$J(x(t), u(t)) = \int_0^1 g(t, x(t), u(t)) dt \rightarrow \inf$$

And we found the necessary conditions for optimal control, by using Lagrange principle.